

# Transparent SNARKs from DARK Compilers

Benedikt Bünz<sup>1</sup> and Ben Fisch<sup>1</sup> and **Alan Szepieniec**<sup>2</sup>

<sup>1</sup>Stanford <sup>2</sup>Nervos Foundation

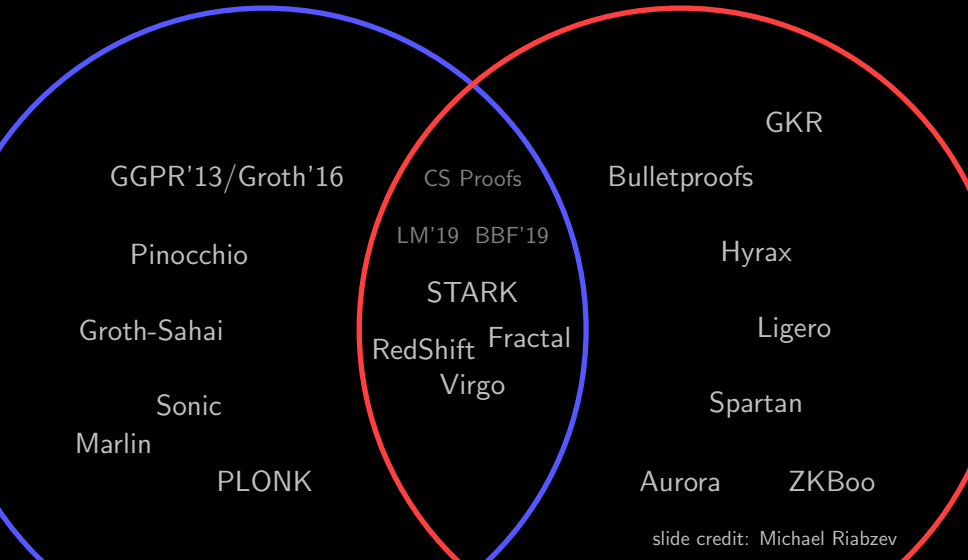
Eurocrypt 2020

# General Purpose Zero-Knowledge Proofs



succinct verification

transparent setup

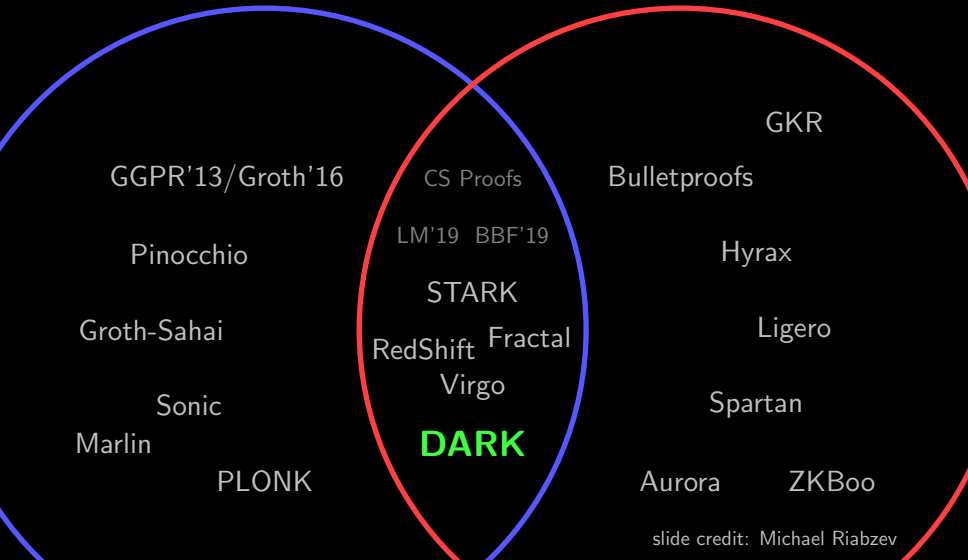


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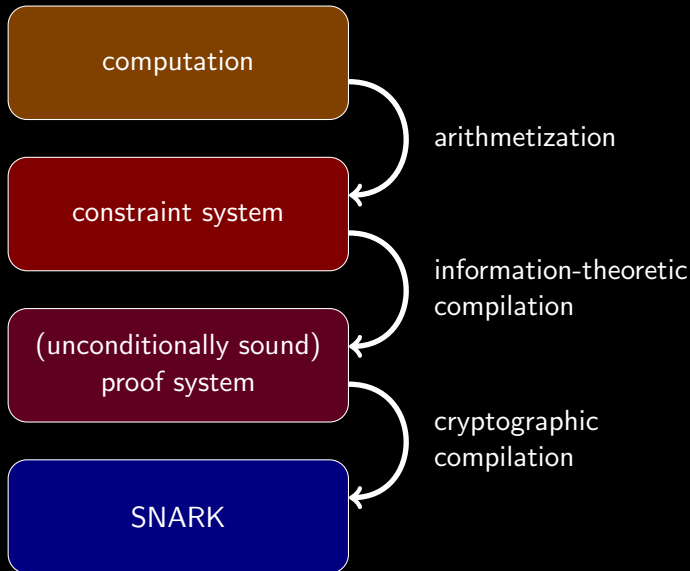


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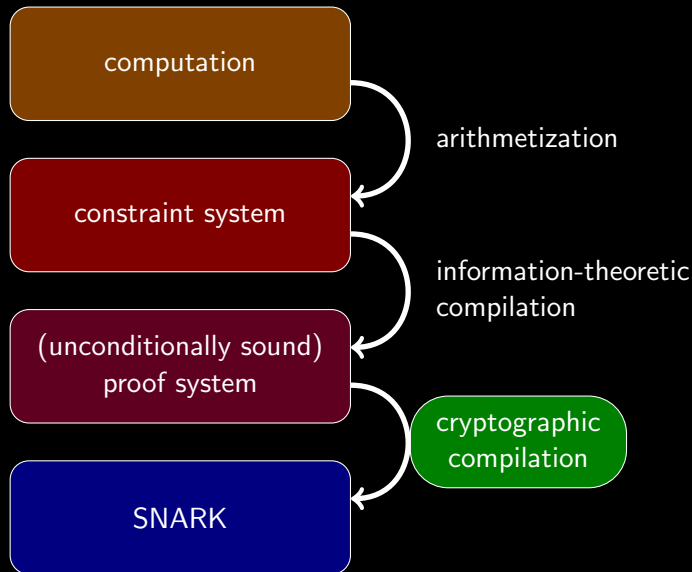
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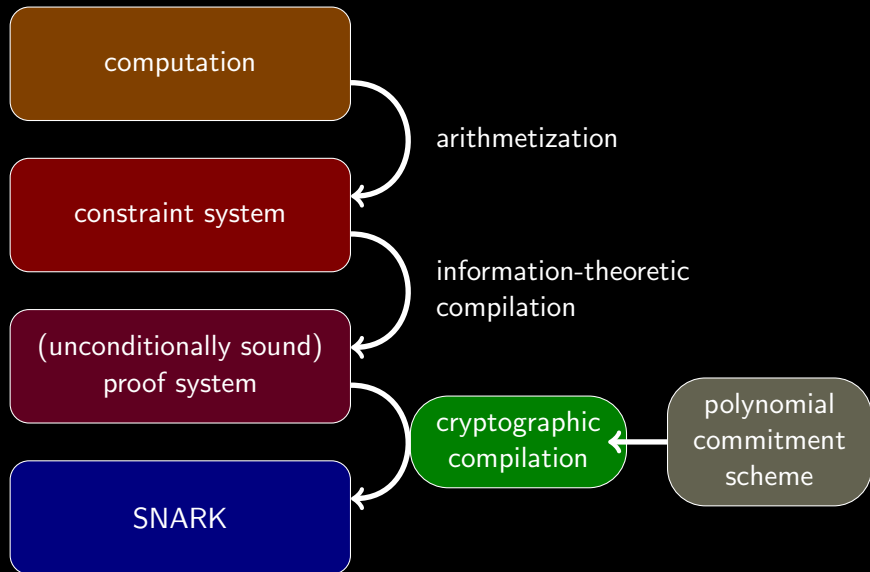
# Compilation Pipeline



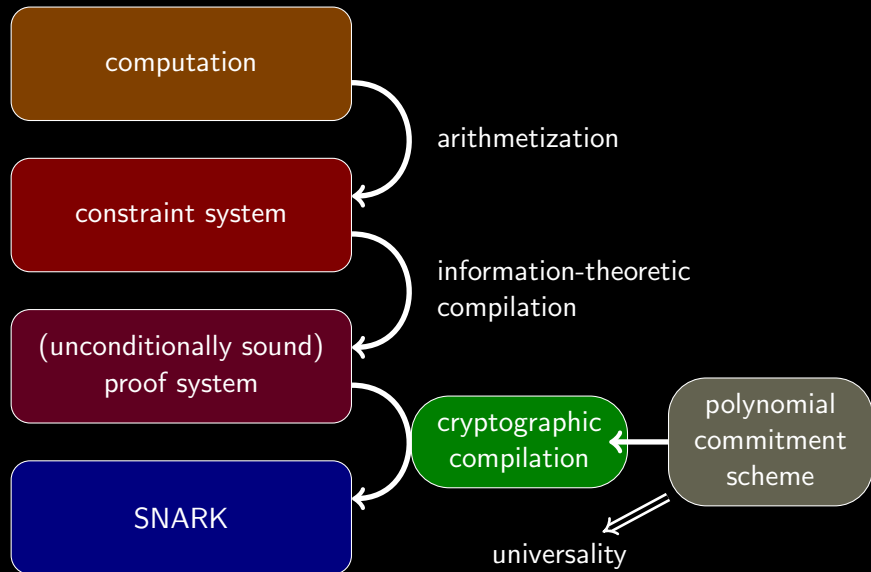
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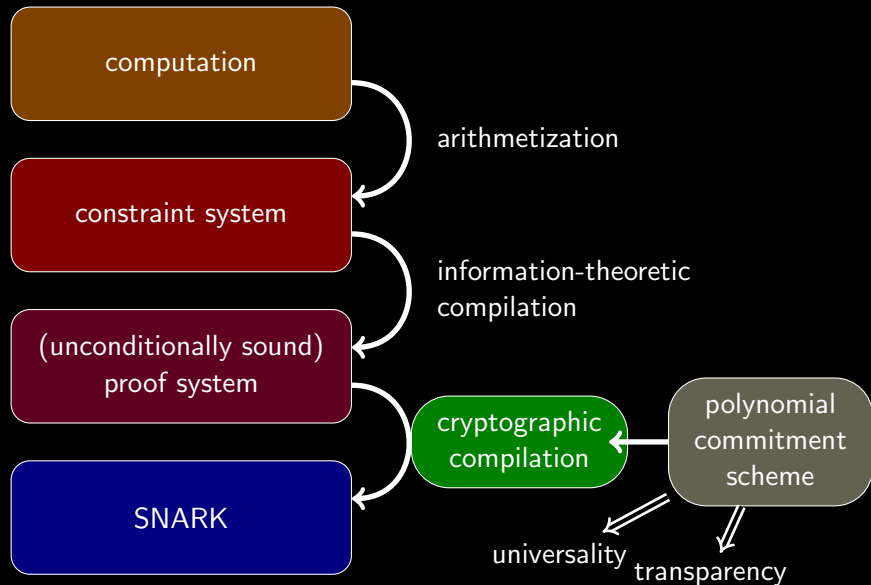
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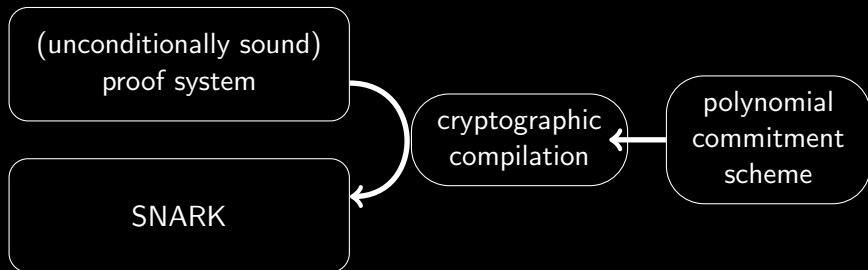


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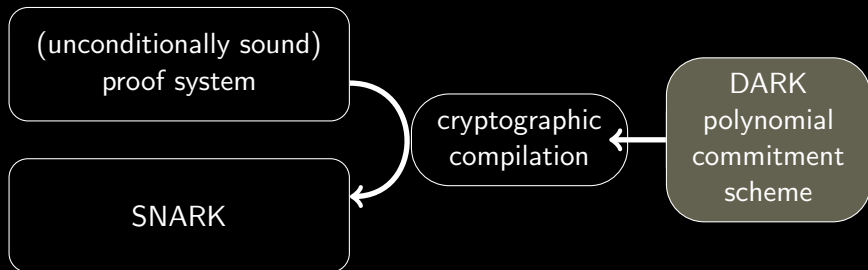
# Contributions



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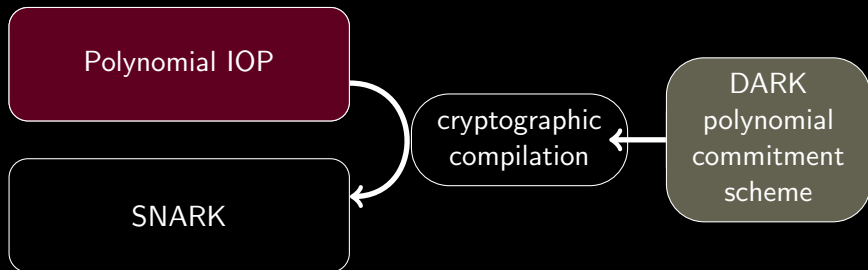
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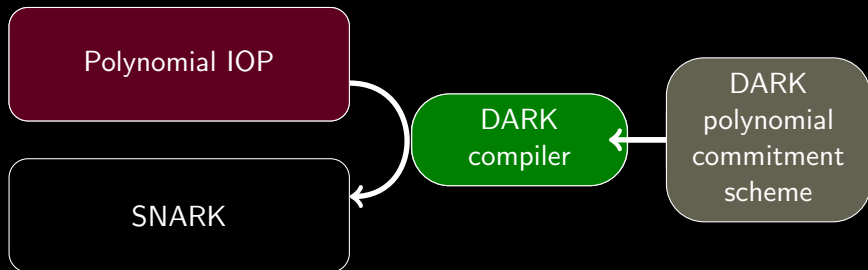
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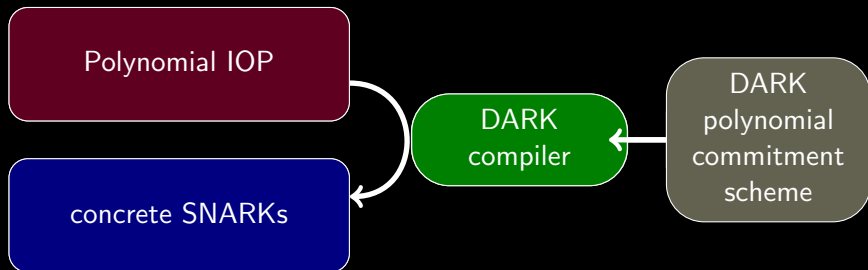
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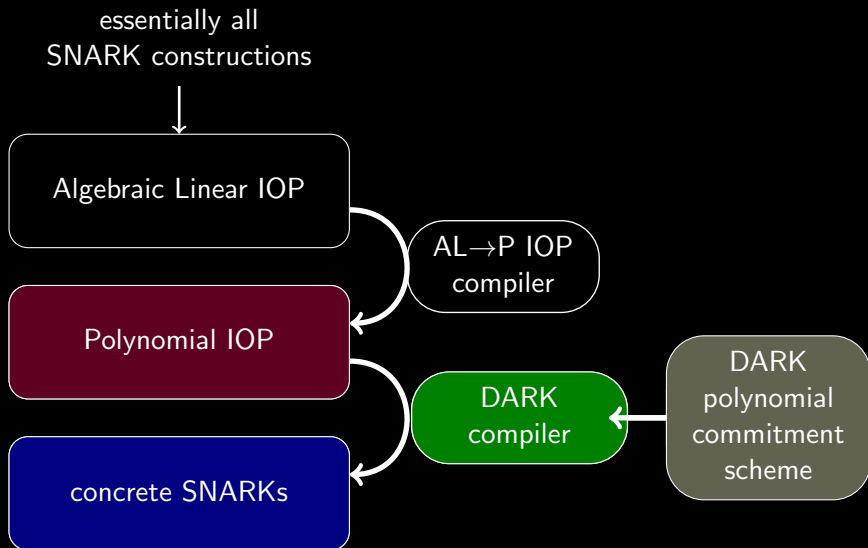
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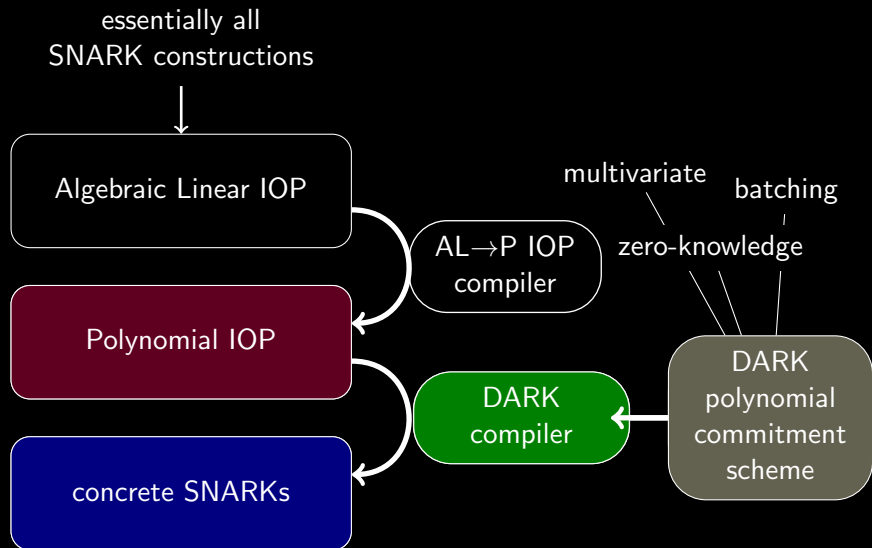
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(and other constructions)



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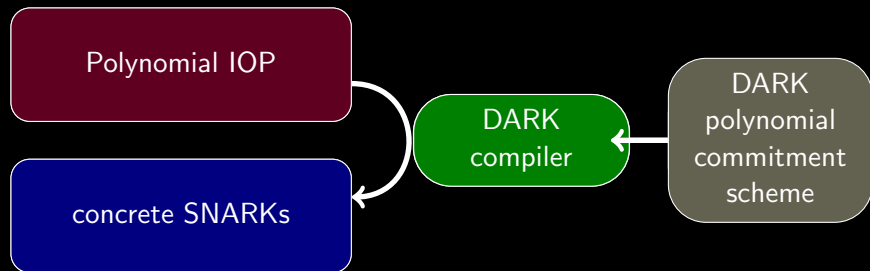
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# Talk Outline



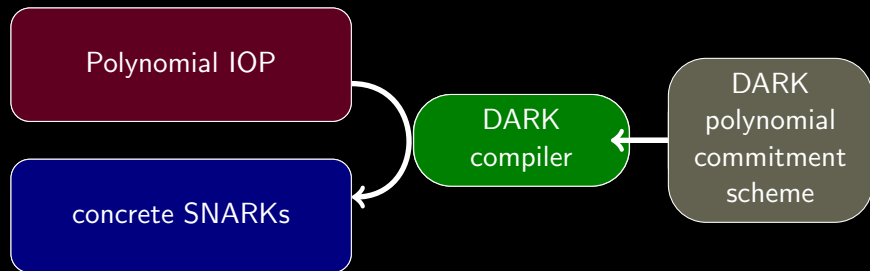
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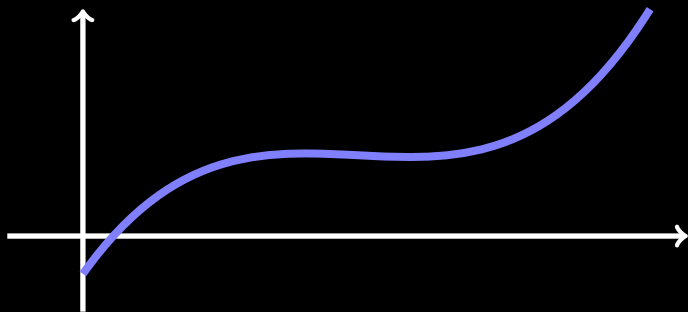




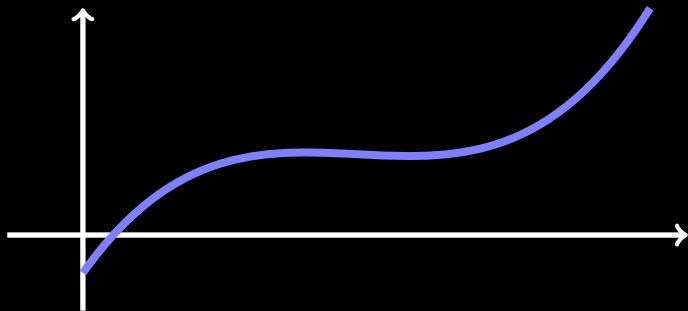
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# Polynomial Commitment Scheme

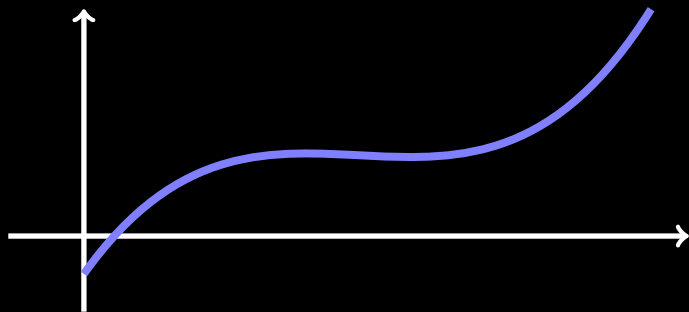


# Polynomial Commitment Scheme



lots of coefficients

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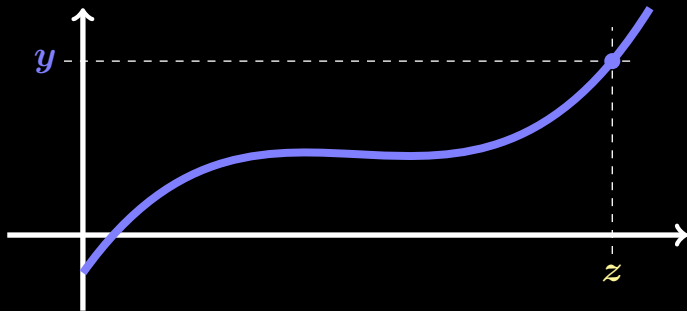


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short commitment

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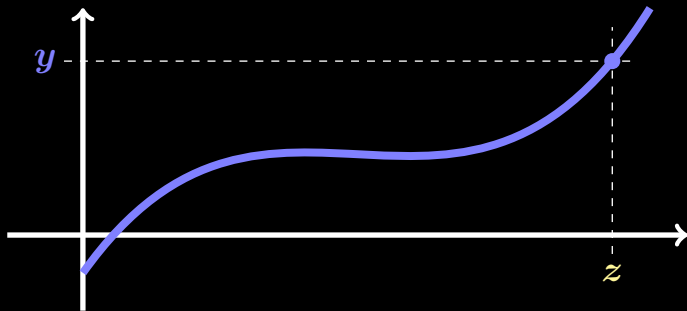
$$f(z) = y$$

evaluation



proof

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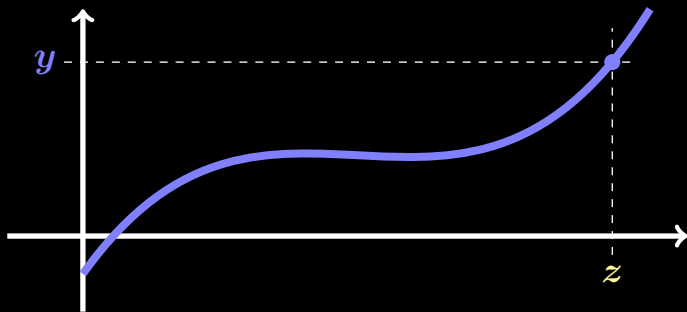
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$\pi$

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← extractable

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# Evaluation Protocol with Special Homomorphic Commitment

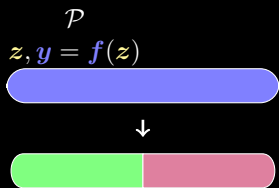


$$\mathcal{P}$$
$$z, y = f(z)$$


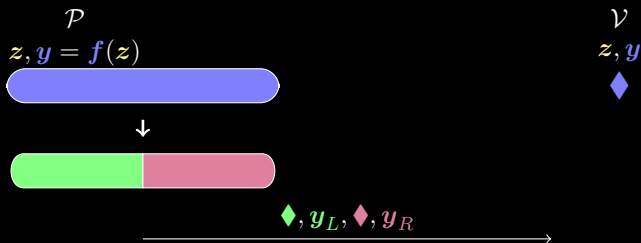
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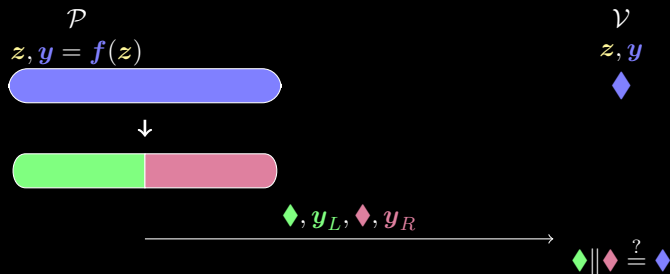

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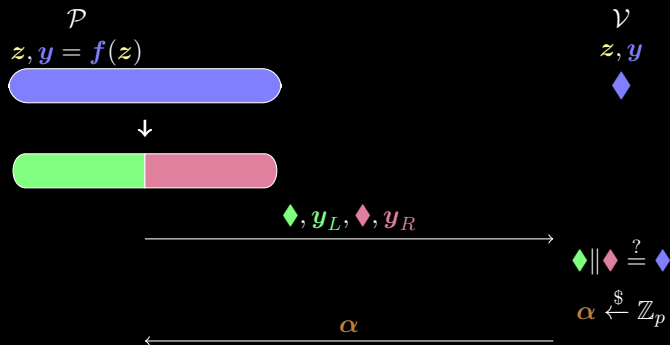
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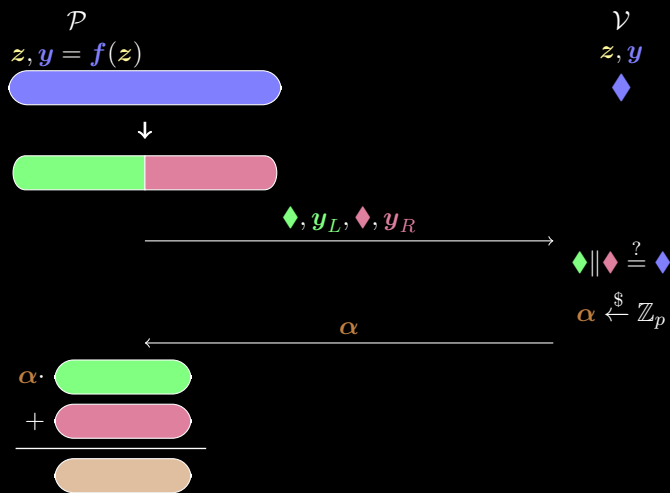
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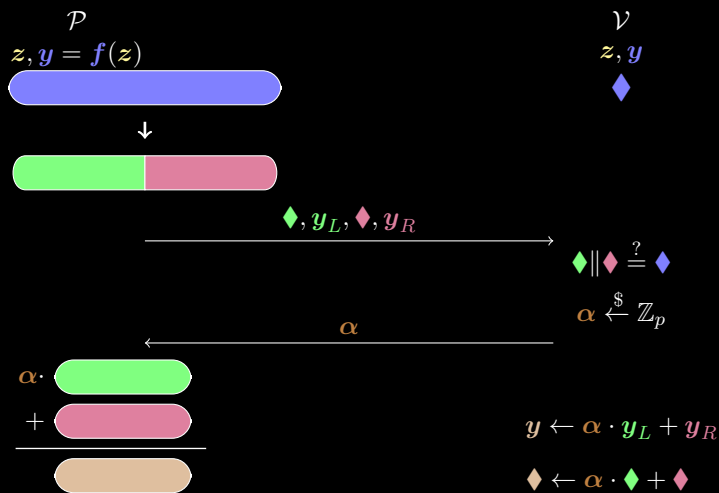
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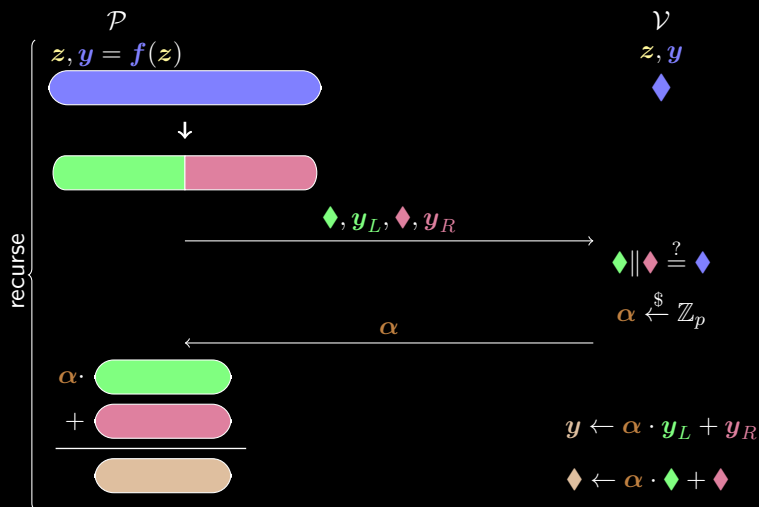
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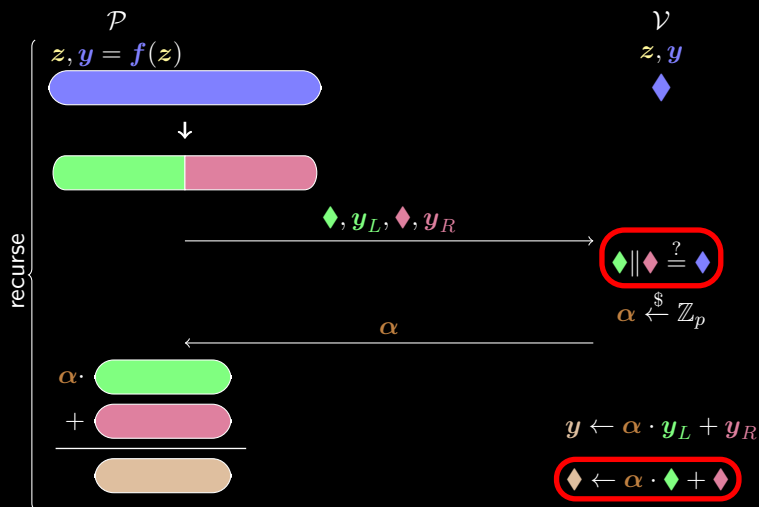
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# Special Homomorphic Commitment ♦





0. commitment to elements from infinite set

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$\rightarrow$  Groups of Unknown Order

# Groups of Unknown Order



## RSA Group

- ▶  $\mathbb{Z}_n^*/\langle -1 \rangle, \times \ n = pq$
- ▶ **big**
- ▶ **trusted setup**

## Class Group

- ▶  $\mathcal{Cl}(\Delta), \times \text{ of } \mathbb{Q}(\sqrt{\Delta})$
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not post quantum



# Hardness Assumptions



Strong RSA Assumption:

$$g \xleftarrow{\$} \mathbb{G}$$

$$(u, \ell) \leftarrow \mathcal{A}(g)$$

---

$$\mathcal{A} \text{ wins} \Leftrightarrow u^\ell = g$$

Adaptive Root Assumption:

$$(g, st) \leftarrow \mathcal{A}_0(\mathbb{G})$$

$$\ell \xleftarrow{\$} \text{Primes}(\lambda 2^\lambda)$$

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falsifiable ✓

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polynomial equations

*over the integers*

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Diophantine Arguments of Knowledge

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"I know  $\mathbf{y} \in \mathbb{Z}^m$   
such that  $\mathcal{P}(\mathbf{x}, \mathbf{y}) = 0$ "

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\*: if  $q$  is large enough

# Commitment



0. commitment

1. compute linear relations:  $\diamond \leftarrow \alpha \cdot \blacklozenge + \blacklozenge$

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---

Wesolowski 2019: PoE (proof of exponentiation)

$\mathcal{P}$  claim:  $u^x = v$   $\mathcal{V}$

$\ell \stackrel{\$}{\leftarrow} \text{Primes}(\lambda \cdot 2^{2\lambda})$

---

$q = \lfloor x/\ell \rfloor \quad r = x \bmod \ell$

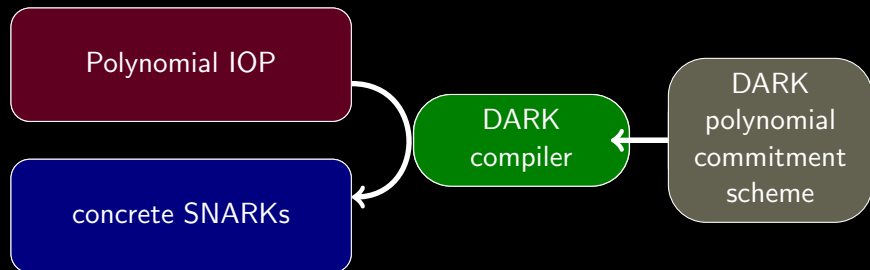
$Q = u^q$

---

$Q^\ell u^r \stackrel{?}{=} v$

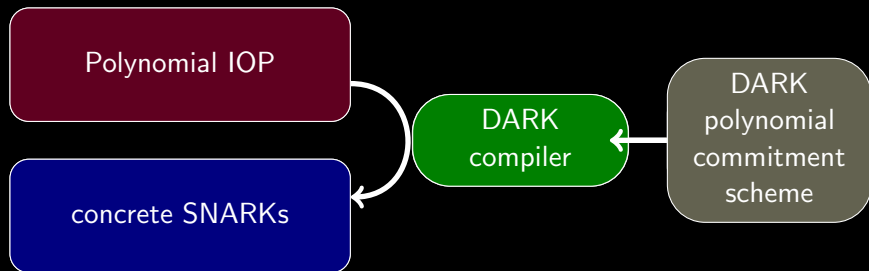


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(and other constructions)





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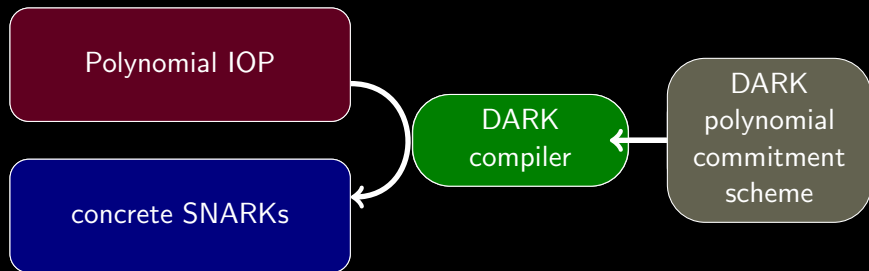




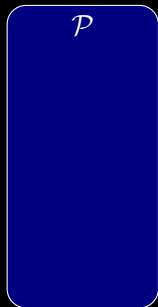
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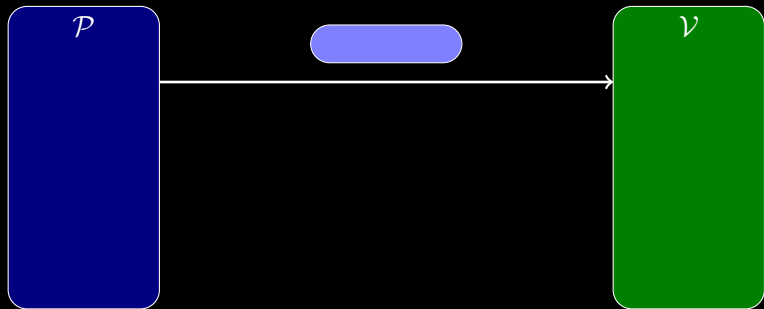
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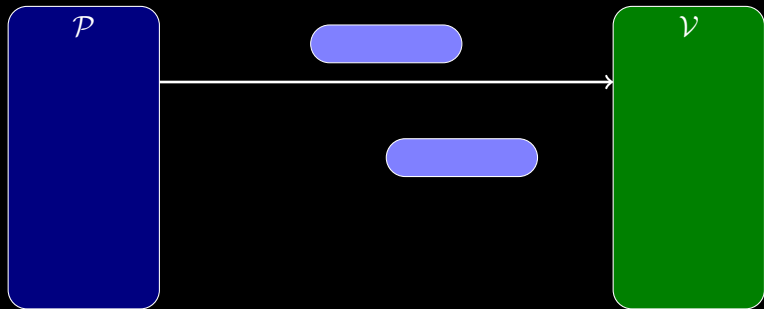
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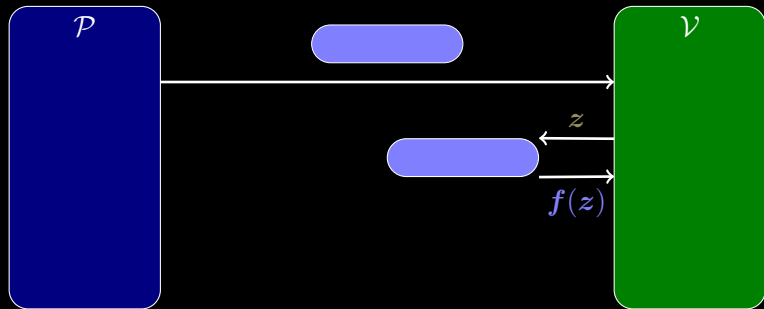
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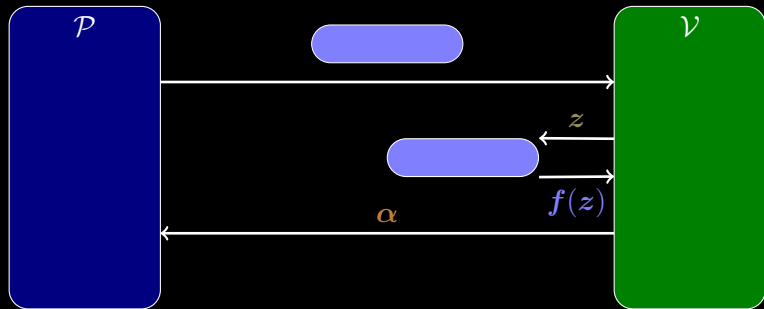
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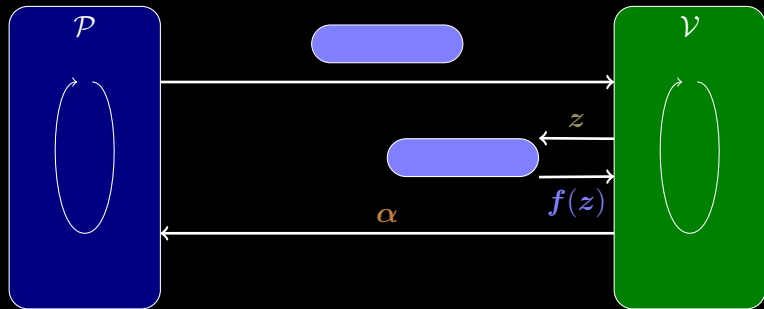
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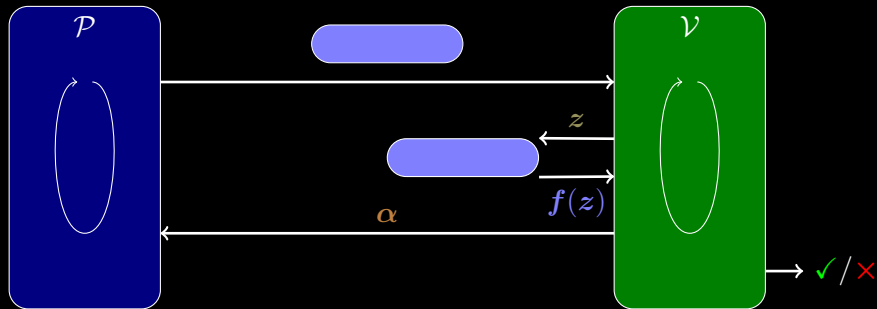
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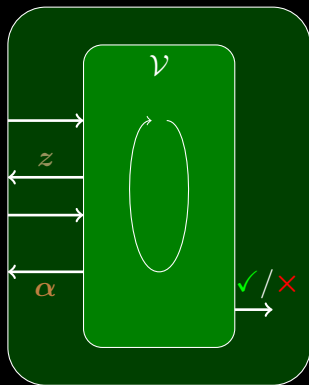
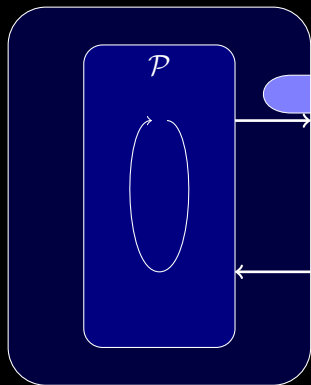


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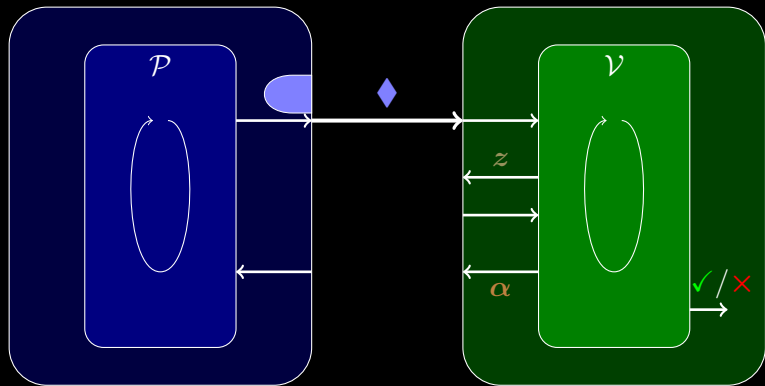




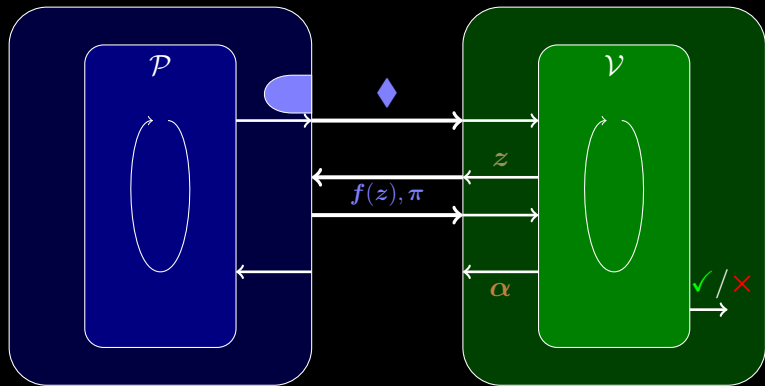
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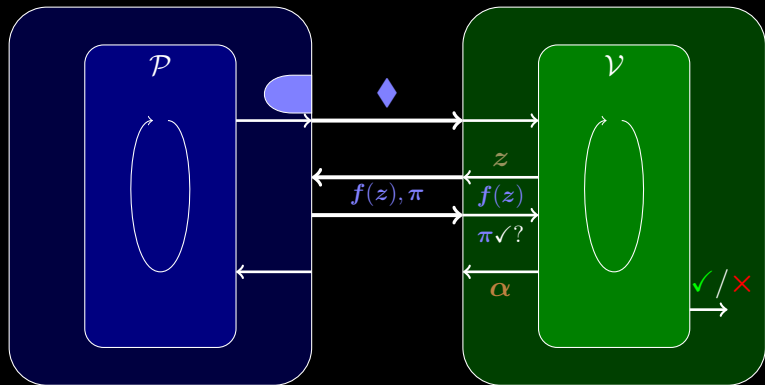
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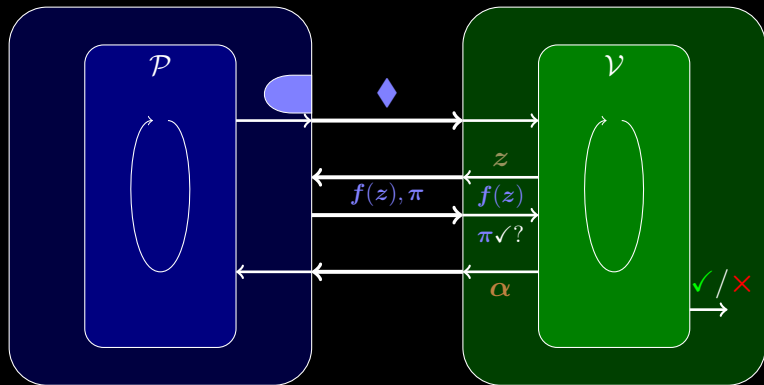
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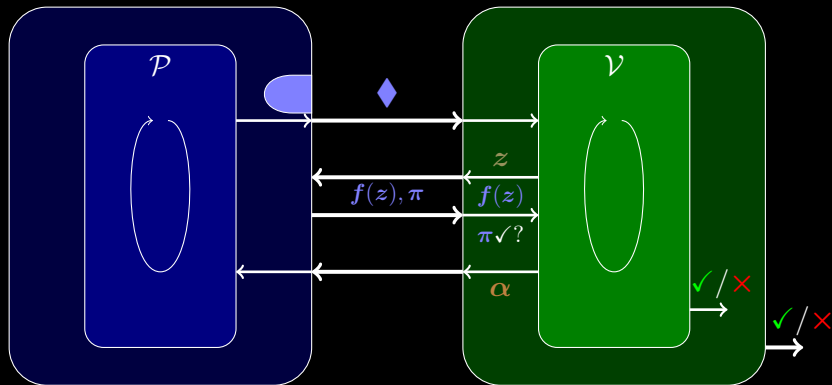
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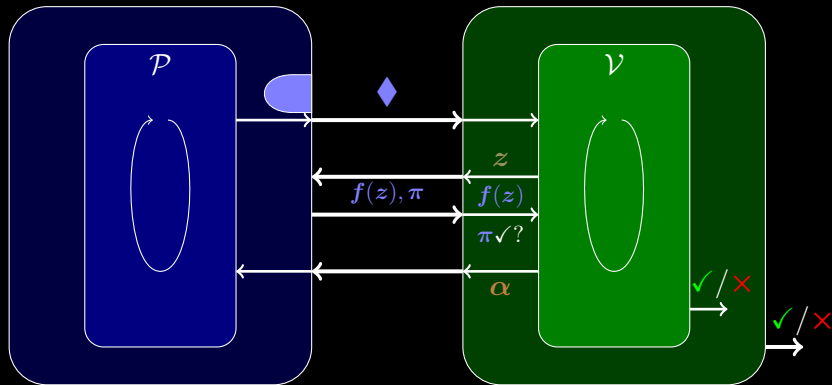
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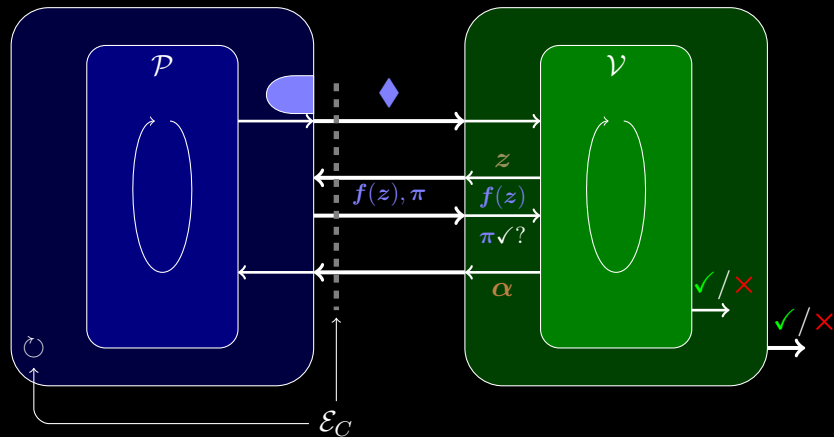
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# Compiled Polynomial IOP — Soundness

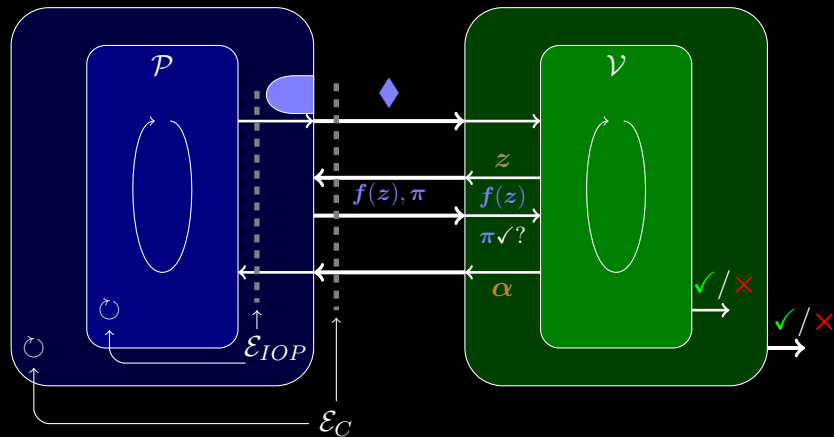


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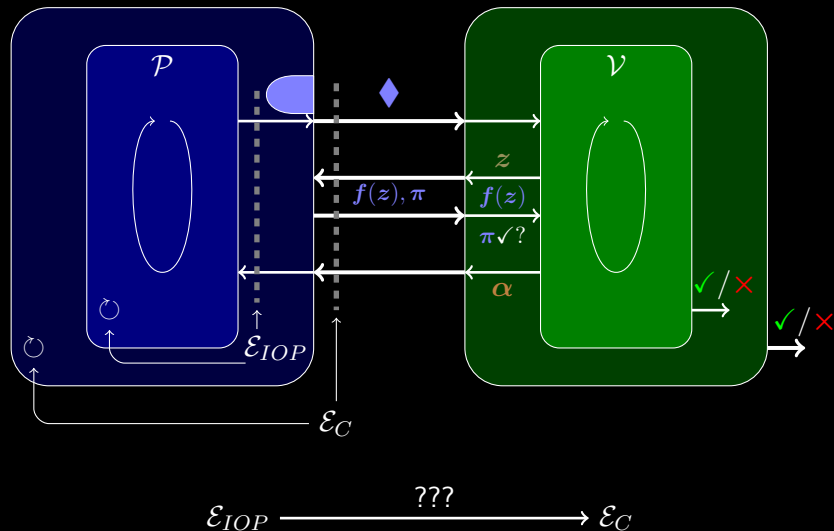




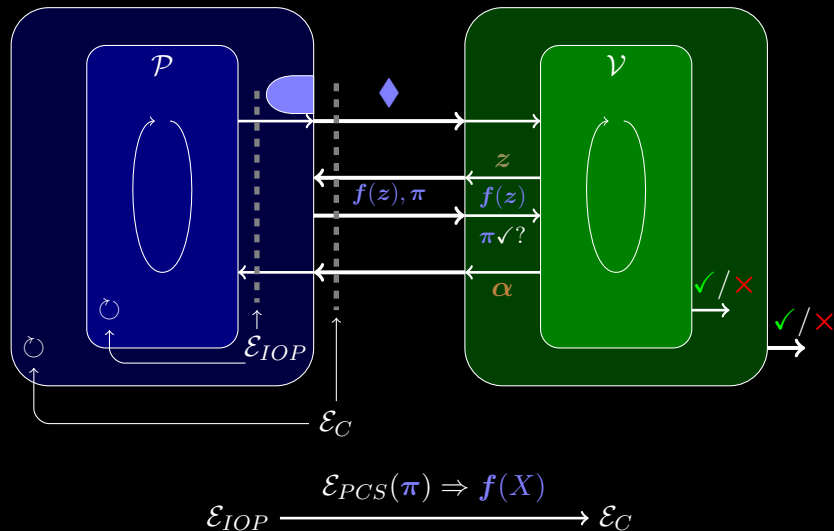
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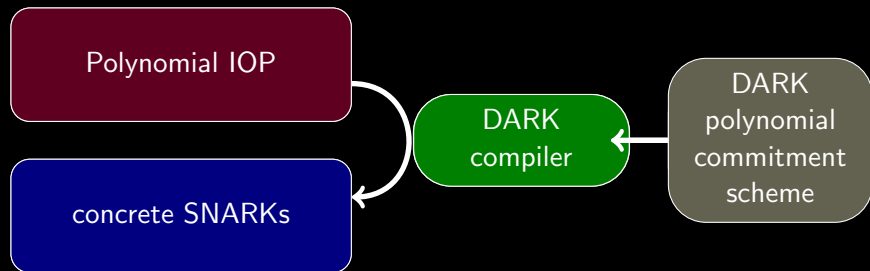
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# Talk Outline



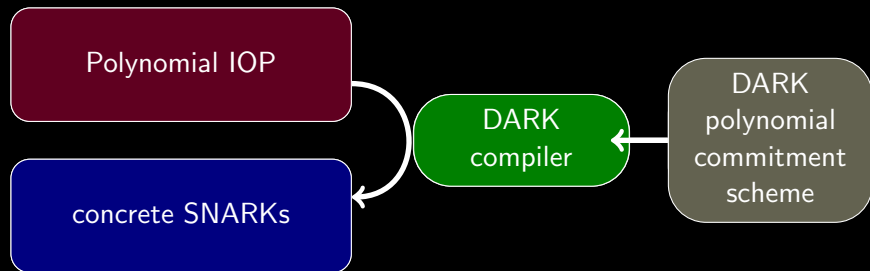
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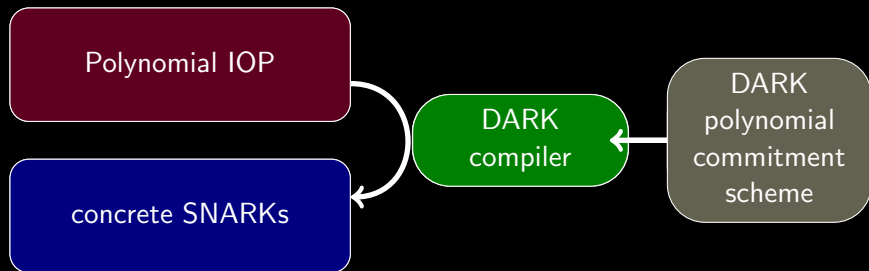
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# Supersonic / Other Constructions



$$\begin{array}{r} \text{Sonic-IOP} \\ + \text{KZG PCS} \\ \hline \text{Sonic} \end{array}$$

# Supersonic / Other Constructions





# Supersonic / Other Constructions



Sonic-IOP  
+ KZG PCS

---

Sonic

Sonic-IOP  
+ DARK PCS

---

Supersonic

PLONK-IOP  
+ KZG PCS

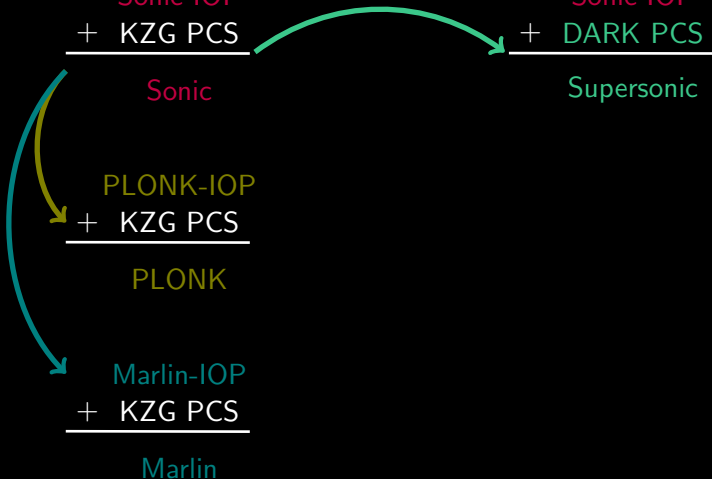
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PLONK

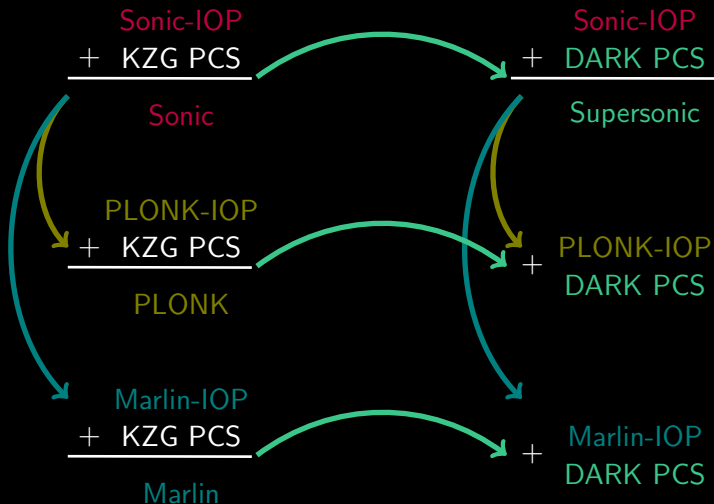
Marlin-IOP  
+ KZG PCS

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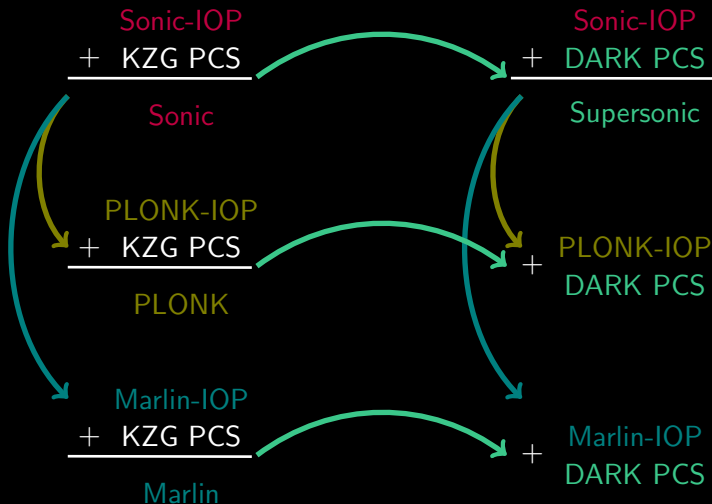
Marlin



# Supersonic / Other Constructions



# Supersonic / Other Constructions



transparent setup (class groups)  
constant-size SRS (RSA groups)

# Supersonic Performance



Polynomial IOP	# Polynomials	# Eval points	$ \pi $
Sonic	12 + 15	12	15.3 KB
PLONK	7 + 7	2	10.1 KB
Marlin	9 + 10	3	12.3 KB

Scheme	Transp.	CRS	Prover	Verifier	$ \pi $	$ \pi $
Supersonic	✓	1	$n \log(n)$	$3 \log(n)$	$2 \log(n)$	10.1KB
PLONK	×	$2n$	$n$	1	1	720b
Groth16	×	$2n$	$n$	1	1	192b
Bulletproofs	✓	$2n$	$n$	$n$	$2 \log(n)$	1.7KB
STARK	✓	1	$\lambda T$	$\lambda \log^2(T)$	$\lambda \log^2(T)$	600 KB
Virgo	✓	1	$\lambda n$	$\lambda \log^2(n)$	$\lambda \log^2(n)$	271 KB

concrete quantities for  $n = 2^{20}$  and  $\lambda = 120$

# Conclusions



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  - ▶ all SNARKs have a DARK analogue

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  - ▶ Polynomial IOPs
  - ▶ multi-round Fiat-Shamir
  
- ▶ Future work:
  - ▶ improvements
  - ▶ implementation



# Thank you!

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`https://eprint.iacr.org/2019/1229`

